

Model-free analysis for large proteins at high magnetic field strengths

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Received: 30 March 2007 / Accepted: 21 May 2007 / Published online: 26 June 2007
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Abstract Protein backbone dynamics is often characterized using model-free analysis of three sets of ^{15}N relaxation data: longitudinal relaxation rate (R_1), transverse relaxation rate (R_2), and ^{15}N -{H} NOE values. Since the experimental data is limited, a simplified model-free spectral density function is often used that contains one Lorentzian describing overall rotational correlation but not one describing internal motion. The simplified spectral density function may be also used in estimating the overall rotational correlation time, by making the R_2/R_1 largely insensitive to internal motions, as well as used as one of the choices in the model selection protocol. However, such approximation may not be valid for analysis of relaxation data of large proteins recorded at high magnetic field strengths since the contribution to longitudinal relaxation from the Lorentzian describing the overall rotational diffusion of the molecule is comparably small relative to that describing internal motion. Here, we quantitatively estimate the errors introduced by the use of the simplified spectral density in model-free analysis for large proteins at high magnetic field strength.

Keywords NMR · Relaxation · Rotational correlation time · Protein · Dynamics

Introduction

NMR relaxation is often applied to characterize protein internal motion (Bruschweiler 2003; Dayie et al. 1996; Fushman and Cowburn 2001; Igumenova et al. 2006; Ishima and Torchia 2000; Jarymowycz and Stone 2006; Kay 2005; Palmer 2001; Redfield 2004). To evaluate internal motion on the sub-nanosecond time scale, model-free analysis is one of the most frequently used approaches (Lipari and Szabo 1982). Particularly in the characterization of backbone dynamics of proteins, three types of ^{15}N relaxation data, longitudinal (R_1), transverse relaxation rates (R_2), and ^{15}N -{H} NOE are typically used in the analysis to optimize the model-free parameters by χ^2 minimization of a target function (Clare et al. 1990; Kay et al. 1989; Mandel et al. 1995; Palmer et al. 1991; Schneider et al. 1992). Although inclusion of other relaxation data sets, such as cross-correlation relaxation rates, auto-relaxation rates at different static or effective magnetic field strengths, or relaxation rates for different nuclei, is useful for optimization of model-free parameters (Campbell et al. 2000; Fushman et al. 1999; Idiyatullin et al. 2003; Kroenke et al. 1998; Lee et al. 1997; Pelupessy et al. 2003; Tjandra et al. 1995), the model-free analysis that uses only ^{15}N R_1 , R_2 , and NOE data sets has been most accepted as a global standard for straightforward characterization of protein backbone dynamics.

There are two major steps in the model-free analysis using ^{15}N R_1 , R_2 , and NOE data sets: (1) determination of a rotational correlation time(s) of a molecule (τ_R) and (2) optimization of model-free parameters at individual amide

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sites. In the first step, τ_R value is often optimized by directly calculating it from the average, or trimmed R_2/R_1 ratio since the R_2/R_1 ratio is free from the effects of internal motion for sites that have short correlation time for internal motion (Fushman et al. 1994; Kay et al. 1989; Palmer et al. 1991). Alternatively, τ_R value can be optimized by fitting with a model-free spectral density function for sites that exhibit average R_2/R_1 ratios (Clore et al. 1990; Schneider et al. 1992). In the second step, typically four parameters are optimized for each site: a generalized order parameter (S^2), a correlation time for internal motion (τ_i), a chemical exchange term (R_{ex}) and a generalized order parameter for internal motion much faster than τ_i (S_f^2). This however cannot be done simultaneously with a limited number of experimental data sets. Instead, a model selection protocol is used to select one out of the five models that contain one to three of the four model-free parameters. Although there are several different protocols for model selection, the basic principle of the model-free analysis is similar in all cases (Andrec et al. 1999; Clore et al. 1990; Farrow et al. 1994; Lee and Wand 1999; Mandel et al. 1995; Spyropoulos 2006).

The application of the model-free analysis for backbone dynamics has been mostly optimized for ^{15}N R_1 , R_2 , and NOE data sets acquired at the magnetic field strengths of 11.74 T (500 MHz ^1H) or 14.09 T (600 MHz ^1H). The general protocol for the model-free analysis may not necessarily be suitable for the relaxation data recorded at higher magnetic field strengths, such as 18.8 T (800 MHz ^1H) or higher. In addition, treatment of relaxation data from larger proteins poses an extra challenge since, except for $J(0)$, the magnitude of the spectral density function due to molecular rotation decreases as the molecular size increases. Although many studies have been published to assess the protocols of the model-free analysis and address the accuracy of the obtained parameters (Andrec et al. 1999; Barchi et al. 1994; Chandrasekhar et al. 1992; Chen et al. 2004; d'Auvergne and Gooley 2003; Korchuganov et al. 2004; Korzhnev et al. 1997; Lee and Wand 1999; Meirovitch et al. 2003; Pawley et al. 2001; Schramm et al. 1991; Spyropoulos 2006), none have specifically targeted the large-molecule high-field case. A previous study performed by Tjandra's group commented about errors caused by the use of R_2/R_1 ratio to estimate τ_R , but did not systematically characterize them as a function of the applied magnetic field strength (Chang and Tjandra 2005). Since, spectral density values are dependent on the static magnetic field strength and the rotational correlation time of the molecule, it is important to reexamine the assumptions used in the model-free analysis for large molecules at high magnetic field strengths.

Here, we numerically simulate relaxation rates assuming different spectral density functions, and describe the accuracy of the model-free analysis at high magnetic field strength for large proteins. We show that the use of a simplified spectral density function containing only one Lorentzian introduces potential errors in the analysis, that is, the τ_R value calculated from the average, or trimmed R_2/R_1 ratio tends to be systematically smaller than expected, which in turn results in systematic increases in the S^2 values. Similarly, the use of the one Lorentzian spectral density function will also overestimate NOE values for large proteins, which will increase the number of residues that cannot be optimized by model-free analysis. Although the discrepancies due to one Lorentzian term are negligible if τ_i values are small (< 10 ps), they become significant when the τ_i values are 20–30 ps or more due to the fact that contributions from τ_R and τ_i become comparable. These results are significant as an increasing number of proteins are being studied at high field and as τ_i values of 20–30 ps are rather commonplace even in rigid portions of proteins (Barchi et al. 1994; Chandrasekhar et al. 1992; Farrow et al. 1994; Philippopoulos et al. 1997; Sheinerman and Brooks 1997).

Methods

The relaxation rates can be expressed in terms of the spectral density function, $J(\omega)$, as described below.

$$R_1 = (d^2/10)\{3J(\omega_N) + J(\omega_H - \omega_N) + 6J(\omega_H + \omega_N)\} + c^2J(\omega_N) \quad (1)$$

$$R_2 = (d^2/20)\{4J(0) + 3J(\omega_N) + J(\omega_H - \omega_N) + 6J(\omega_H) + 6J(\omega_H + \omega_N)\} + (c^2/3)\{4J(0) + 3J(\omega_N)\} + R_{ex} \quad (2)$$

$$\text{NOE} = 1 + \{\gamma_H(d^2/10)\sigma_{\text{cross}}\}/(\gamma_N R_1) \quad (3)$$

Here, d^2 and c^2 are coefficients for dipolar and CSA interactions, and, γ_H and γ_N are gyromagnetic ratios of ^1H and ^{15}N , respectively, σ_{cross} is a cross relaxation term given by $(d^2/10)(6J(\omega_H + \omega_N) - J(\omega_H - \omega_N))$, and R_{ex} is the chemical exchange contribution to R_2 value (Cavanagh et al. 1996).

The typical spectral density functions applied in the model-free analysis are the simplified spectral density function, $J_{\text{SMF}}(\omega)$ (Eq. 4), the model-free spectral density function, $J_{\text{MF}}(\omega)$ (Eq. 5), and the extended spectral density function, $J_{\text{EMF}}(\omega)$ (Eq. 6).

$$J_{SMF}(\omega) = S^2 \frac{\tau_R}{(1 + \omega^2 \tau_R^2)} \tag{4}$$

$$J_{MF}(\omega) = S^2 \frac{\tau_R}{(1 + \omega^2 \tau_R^2)} + (1 - S^2) \frac{\tau_e}{(1 + \omega^2 \tau_e^2)} \tag{5}$$

$$J_{EMF}(\omega) = S_f^2 \left[S_s^2 \frac{\tau_R}{(1 + \omega^2 \tau_R^2)} + (1 - S_s^2) \frac{\tau_e}{(1 + \omega^2 \tau_e^2)} \right] \tag{6}$$

Here, $S^2 = S_f^2 S_s^2$ and $\tau_e^{-1} = \tau_R^{-1} + \tau_i^{-1}$. The spin coefficient, $2/5$, is included in c^2 and d^2 terms for simplification. When $J_{SMF}(\omega)$ and $J_{MF}(\omega)$ are employed, there are options to account for chemical exchange (R_{ex}) in R_2 , as described in Eq. 2. Thus, there are a total of five possible combinations of spectral densities to be selected for optimization of the model-free parameters at each amide site. The five spectral densities have the following sets of parameters: (S^2), (S^2, τ_e), (S^2, R_{ex}), (S^2, τ_e, R_{ex}), and (S^2, S_f^2, τ_e).

Approximation of $J_{MF}(\omega)$ by $J_{SMF}(\omega)$ is valid when the condition indicated in Eq. 7 is satisfied at all angular frequencies that contribute to relaxation, i.e., at 0, ω_N , and ω_H . Here, ω_H is used to approximate ($\omega_H + \omega_N$) and ($\omega_H - \omega_N$) because ω_H is ca. 10 times larger than ω_N .

$$S_s^2 \frac{\tau_R}{(1 + \omega^2 \tau_R^2)} \gg (1 - S_s^2) \frac{\tau_e}{(1 + \omega^2 \tau_e^2)} \tag{7}$$

Under condition (7), the R_2/R_1 ratio is independent of S^2 and τ_i and depends solely on ω_i ($i = H$ or N) and τ_R . Therefore, τ_R is directly calculated from R_2/R_1 for the sites which satisfy condition (7) (Fushman et al. 1994; Kay et al. 1989; Palmer et al. 1991). Alternatively, τ_R can be optimized by fitting with the model-free spectral density ($J_{MF}(\omega)$) for the sites that fall around the trimmed mean R_2/R_1 ratio (Clore et al. 1990; Schneider et al. 1992).

In the case of $J(0)$ term, $J_{MF}(\omega)$ is expressed according to Eq. 8.

$$J_{MF}(0) = S_s^2 \tau_R + (1 - S_s^2) \tau_e \tag{8}$$

Therefore, condition (7) is valid simply when $\tau_R \gg \tau_e$. However, in the case of $J_{MF}(\omega)$ at ω_N and ω_H angular frequencies, the validity of condition (7) will also depend on ω and τ_R values.

To investigate errors introduced by the use of simplified $J_{SMF}(\omega)$, we first simulate $\tau/(1 + \omega^2 \tau^2)$ values as a function of the correlation time, τ , at individual ω_N and ω_H frequencies and at 11.74 and 18.8 T. Next, we simulate the relaxation rates expressed by Eqs. 1–3 using both $J_{SMF}(\omega)$ and $J_{MF}(\omega)$ spectral density functions. In the simulations of

relaxation rates, we assume $S^2 = 0.85$, $\tau_i = 10$ ps or 50 ps, and $R_{ex} = 0$. According to previous studies (Barchi et al. 1994; Chandrasekhar et al. 1992; Farrow et al. 1994; Philippopoulos et al. 1997; Sheinerman and Brooks 1997), $\tau_i = 10$ ps should be fast enough to apply $J_{SMF}(\omega)$ whereas $\tau_i = 50$ ps should fall on the border between fast and slow internal motion. NOE values in rigid regions of proteins are often larger than 0.8 when τ_i is 10 ps or faster (Coles et al. 1999; Ding et al. 2005; Garcia et al. 2000; Savard and Gagne 2006; Yuan et al. 1999), but in some cases lower than 0.8 when τ_i values are slower, i.e., $\tau_i > 10$ ps (Abu-Abed et al. 2004; Bouamr et al. 2005; Fausti et al. 2001; Zhuravleva et al. 2004). To test the effects of static magnetic field strength, simulations were performed at 11.74 T (500 MHz 1H) and 18.8 T (800 MHz 1H). The simulated results are shown as a function of a rotational correlation time, τ_R . Simulations were performed using MATLAB (The Mathworks Inc., Natick, MA).

Results and discussion

Angular frequency dependence of the $\tau/(1 + \omega^2 \tau^2)$ term

The purpose of this manuscript is to determine whether the $J_{SMF}(\omega)$ can be safely applied as a simplified form of $J_{MF}(\omega)$ for large proteins at high magnetic field strengths. For this purpose, we do not assume molecular anisotropy, chemical exchange, or experimental noise error, but simply compare differences in relaxation values calculated using $J_{SMF}(\omega)$ (Eq. 4) and $J_{MF}(\omega)$ (Eq. 5). Prior to the comparison of relaxation rates, it is useful to estimate the ranges of the correlation time that satisfy the condition (7). To do so, $\tau/(1 + \omega^2 \tau^2)$ is plotted as a function of a general correlation time, τ , at individual ω_N and ω_H at 11.74 T and compared to $\tau/(1 + \omega^2 \tau^2)$ at 18.8 T (Fig. 1).

Figure 1 shows that at 10 ns overall correlation time, which corresponds roughly to a protein of 20 kDa at 25 °C (Dayie et al. 1996), the $J(\omega_N)$ at 18.8 T is only 40% of the $J(\omega_N)$ at 11.74 T. This is because the magnitude of the spectral density function is reduced when the magnetic field strength increases. On the other hand, for short correlation times, i.e., $\omega_N \tau \ll 1$, $J(\omega_N)$ is determined by the τ term and is independent of the value of ω_N . Such observations indicate that once the static magnetic field increases, the magnitude of $\tau_R/(1 + \omega_N^2 \tau_R^2)$ term (left term in condition (7)) decreases relative to $\tau_e/(1 + \omega_N^2 \tau_e^2)$ (right term in condition (7)) in $J_{MF}(\omega_N)$, suggesting that quantitative investigation of the validity of $J_{SMF}(\omega)$ is required. For example, the simulation shows that when $\tau_R = 10$ ns, $\tau_i = 50$ ps, and $S^2 = 0.85$, the $(1 - S^2) \tau_e / (1 + \omega_N^2 \tau_e^2)$ term is only 1.1% of the $S^2 \tau_R / (1 + \omega_N^2 \tau_R^2)$ at 11.74 T, whereas it is 2.8% at 18.8 T. Similarly, when the value of τ_R increases,

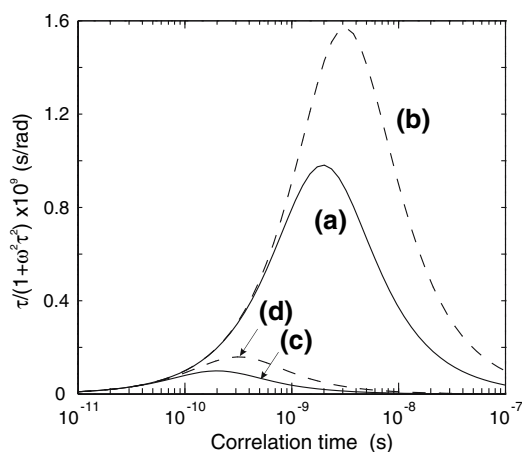


Fig. 1 Values of $\tau/(1 + \omega^2 \tau^2)$ term as a function of the correlation time, τ , (a) for $\omega = \omega_N$ at 18.8 T, (b) for $\omega = \omega_N$ at 11.74 T, (c) for $\omega = \omega_H$ at 18.8 T, and (d) for $\omega = \omega_H$ at 11.74 T

the magnitude of $\tau_R/(1 + \omega_N^2 \tau_R^2)$ decreases: at $\tau_R = 20$ ns, $\tau_i = 50$ ps, $S^2 = 0.85$, the $(1 - S^2)\tau_e/(1 + \omega_N^2 \tau_e^2)$ term becomes 1.8% of the $S^2 \tau_R/(1 + \omega_N^2 \tau_R^2)$ at 11.74 T, whereas it is 4.4% at 18.8 T.

In the case of the $J(\omega_H)$ term, condition (7) is not satisfied unless $\tau_i < 1$ ps and $\tau_R < 5$ ns. Nevertheless, $J_{SMF}(\omega)$ is appropriate since the overall $J(\omega_H)$ contributes little compared to $J(\omega_N)$ and $J(0)$ in R_1 and R_2 (Eqs. 1 and 2, respectively) since ω_H is ca. 10 times ω_N . However, the difference between $J_{SMF}(\omega_H)$ and $J_{MF}(\omega_H)$ is almost equivalent to that of $J_{SMF}(\omega_N)$ and $J_{MF}(\omega_N)$.

These observations suggest that there might be systematic errors caused by the optimization of model-free parameters using $J_{SMF}(\omega)$. This follows from the fact that although contributions from the $J(0)$, $J(\omega_N)$, and $J(\omega_H)$ term are different in the relaxation rates, the $S^2 \tau_R/(1 + \omega_N^2 \tau_R^2)$ term in the use of $J_{SMF}(\omega)$ has to compensate for the neglect of the $(1 - S^2)\tau_e/(1 + \omega_H^2 \tau_e^2)$ term when condition (7) is not satisfied. Since τ_R is a global parameter, the use of $J_{SMF}(\omega)$ eventually leads to an overestimation of S^2 value when condition (7) is not satisfied.

R_1 values simulated using $J_{SMF}(\omega)$ and $J_{MF}(\omega)$

To understand how relaxation rates are dependent on the choice of the spectral density function, we simulated R_1 values (Eq. 1) using $J_{SMF}(\omega)$ and $J_{MF}(\omega)$. In this simulation, relaxation rates are shown as a function of τ_R in which τ_i and S^2 are assumed to be 50 ps and 0.85, respectively. Simulations were done at both 11.74 and 18.8 T.

Figure 2a shows that R_1 values calculated assuming $J_{SMF}(\omega)$, R_1^{SMF} , are slightly smaller than those of $J_{MF}(\omega)$, R_1^{MF} , due to the loss of $(1 - S^2)\tau_e/(1 + \omega_N^2 \tau_e^2)$ term. However, the overall profile of R_1^{SMF} values as a function of τ_R is similar to that of R_1^{MF} . Relative differences in R_1^{SMF}

and R_1^{MF} become larger at higher τ_R values due to the reduction of R_1 value as a function of τ_R at $\tau_R > 3$ ns (Fig. 2a). Similar profiles are observed at both 11.74 and 18.8 T.

To evaluate the differences in R_1^{SMF} and R_1^{MF} more quantitatively, the relative difference, $(R_1^{SMF} - R_1^{MF})/R_1^{MF}$, is shown at $\tau_i = 10$ ps and 50 ps in Fig. 3. At $\tau_i = 10$ ps, which has been “safely” assumed to be the time constant of internal motion in the rigid regions of proteins (Fig. 3a), the $(R_1^{SMF} - R_1^{MF})/R_1^{MF}$ is ca. 1% at 11.74 T but increases to 2.5% at 18.8 T when $\tau_R = 20$ ns. The 2.5% error is comparable to the experimental errors in R_1 . Such results demonstrate that the use of $J_{SMF}(\omega)$ is valid at low magnetic field strength, but becomes marginal at the high magnetic field strength.

Although it is often assumed that fast internal motion on the time scale of $\tau_i < 20$ ps can be neglected, (Barchi et al. 1994; Chandrasekhar et al. 1992; Mandel et al. 1995), there is experimental evidence showing internal motions on the time scale of 20–50 ps in the core regions of some proteins (Farrow et al. 1994; Sheinerman and Brooks 1997; Stone et al. 1993). Thus, it is important to account for the bias introduced into the relaxation rates when $J_{SMF}(\omega)$ is used in the analysis. As anticipated, $(R_1^{SMF} - R_1^{MF})/R_1^{MF}$ values at $\tau_i = 50$ ps (Fig. 3b) becomes larger than those at $\tau_i = 10$ ps (Fig. 3a). At 11.74 T, the $(R_1^{SMF} - R_1^{MF})/R_1^{MF}$ values are 2.6% and 5.0% at $\tau_R = 10$ and 20 ns, respectively. At 18.8 T, the $(R_1^{SMF} - R_1^{MF})/R_1^{MF}$ become 5.2% and 9.6% at $\tau_R = 10$ and 20 ns, respectively. It is noteworthy that bias introduced by $J_{SMF}(\omega)$ is significant at higher magnetic field (18.8 T) even when $\tau_i < 50$ ps (Table 1).

NOE values simulated using $J_{SMF}(\omega)$ and $J_{MF}(\omega)$

More severe differences in the use of $J_{SMF}(\omega)$ and $J_{MF}(\omega)$ are shown for $^{15}\text{N}\{-^1\text{H}\}$ NOE values (Fig. 2b). The discrepancies between NOE values calculated using $J_{SMF}(\omega)$, NOE^{SMF} , and NOE values calculated using $J_{MF}(\omega)$, NOE^{MF} increase significantly as a function of τ_R (Fig. 2b). This is likely because the NOE values are largely influenced by $J(\omega_H)$ terms as shown in Eq. 3. As discussed in the previous section, the $(1 - S^2)\tau_e/(1 + \omega_H^2 \tau_e^2)$ term can easily become larger than $S^2 \tau_R/(1 + \omega_H^2 \tau_R^2)$ at τ_i larger than 1 ps when the spectral density function is evaluated at ω_H .

Differences in the NOE values, $(\text{NOE}^{SMF} - \text{NOE}^{MF})/\text{NOE}^{MF}$, shown in Fig. 4a, clearly indicate that even when $\tau_i = 10$ ps at 11.74 T, NOE^{SMF} differs from NOE^{MF} by 3% and 5% at $\tau_R = 10$ and 20 ns, respectively. At 18.8 T, the NOE^{SMF} differs from NOE^{MF} by 10% at $\tau_R = 20$ ns. Furthermore, when $\tau_i = 50$ ps (Fig. 4b), the NOE^{SMF} differs from NOE^{MF} by more than 10% and 30% at 11.74 T and 18.8 T, respectively, even at $\tau_R = 10$ ns. Although NOE

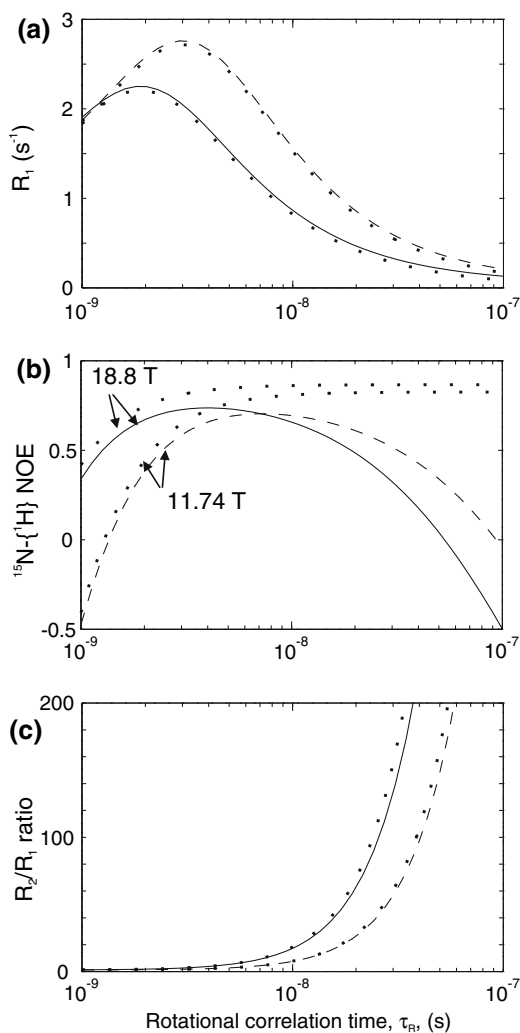


Fig. 2 (a) R_1 , (b) $^{15}\text{N}\{-^1\text{H}\}$ NOE, and (c) R_2/R_1 ratio simulated at 18.8 T (solid line) and 11.74 T (dashed line) as a function of the rotational correlation time, τ_R . In each graph, the values are calculated assuming $J_{\text{MF}}(\omega)$ (solid or dashed lines) and $J_{\text{SMF}}(\omega)$ (dotted lines). Other simulation parameters are $S^2 = 0.85$, $\tau_i = 50$ ps, and $R_{\text{ex}} = 0$

data typically contains larger uncertainties than those in R_1 and R_2 due to the lower sensitivity of the experiment, the more than 10% difference in the NOE values will clearly influence optimization of the model-free parameters. Such results indicate that many residues may not be fit using the $J_{\text{SMF}}(\omega)$ model when relaxation data is collected at the high magnetic field strength.

Parameter dependence of NOE values is shown in Eq. 9 (Kay et al. 1989).

$$\text{NOE}_{\text{MF}} \approx \text{NOE}_{\text{iso}} - \frac{50(1 - S^2)}{(3 + \delta)S^2} \tau_i \tau_m \omega_N^2 \quad (9)$$

Here, NOE_{MF} is the NOE value calculated using $J_{\text{MF}}(\omega)$ given by Eq. 5, whereas NOE_{iso} indicates the NOE value

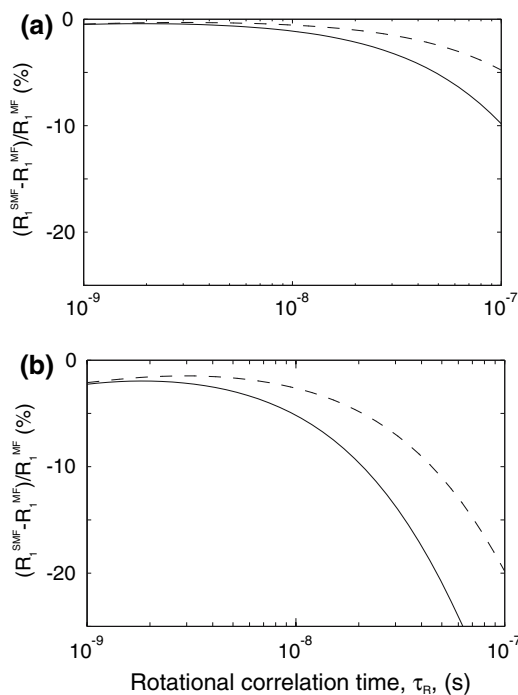


Fig. 3 Percentage difference of R_1 values, $(R_1^{\text{SMF}} - R_1^{\text{MF}})/R_1^{\text{MF}}$, assuming at (a) $\tau_i = 10$ ps and (b) 50 ps. Solid lines are those calculated at 18.8 T, and dashed lines are those calculated at 11.74 T. R_1^{SMF} and R_1^{MF} indicates R_1 values calculated using $J_{\text{SMF}}(\omega)$ and $J_{\text{MF}}(\omega)$, respectively. S^2 and R_{ex} were assumed to be 0.85 and 0, respectively

under conditions of isotropic tumbling, i.e., at $S^2 = 1$. δ indicates ratio of chemical shift anisotropy and dipolar interaction, $(c/d)^2$. Equation 9 has been derived under the assumptions that $\omega_{\text{H}} \pm \omega_{\text{N}} \sim \omega_{\text{H}}$, $(\omega_{\text{H}} \tau_i)^2 \ll 1$ and $(\omega_{\text{N}} \tau_R)^2 \gg 1$ (Kay et al. 1989). Based on this equation, it is clear that NOE values will be reduced at higher magnetic field strengths or at slower rotational correlation times. Thus, when residues used for the estimation of the rotational correlation time are selected based on NOE values, such NOE cut-off should be set lower than usual for experiments conducted for large molecules at high field. This has the adverse effect that it becomes more difficult to distinguish variation in NOE values in rigid regions of proteins from reduced NOE values caused by slow internal motion.

R_2/R_1 values simulated using $J_{\text{SMF}}(\omega)$ and $J_{\text{MF}}(\omega)$

Based on the previous results that R_1^{SMF} is ca. 5% different from R_1^{MF} at 18.8 T and $\tau_R = 20$ ns, it is expected that R_2/R_1 values calculated using $J_{\text{SMF}}(\omega)$, $R_2^{\text{SMF}}/R_1^{\text{SMF}}$, would differ from those calculated using $J_{\text{MF}}(\omega)$, $R_2^{\text{MF}}/R_1^{\text{MF}}$. As shown in Fig. 2c, the R_2/R_1 ratio increases as a function of τ_R , which of course is due to the fact that R_2 increases and R_1 decreases as a function of τ_R . Figure 2c further shows

Table 1 Calculated relaxation values at various correlation times for internal motion^a

τ_i (ps)	R_1 (s ⁻¹)	Diff. (%) ^b	R_2 (s ⁻¹)	Diff. (%)	NOE	Diff. (%)	R_2/R_1	Diff. (%)
11.74 T (500 MHz)								
0	0.816	–	22.50	–	0.821	–	27.5	–
10	0.824	–0.97	22.51	–0.04	0.777	5.66	27.3	0.732
20	0.833	–2.0	22.52	–0.09	0.733	12.0	27.0	1.85
30	0.841	–3.0	22.52	–0.09	0.691	18.8	26.8	2.61
18.8 T (800 MHz)								
0	0.423	–	29.19	–	0.865	–	69.0	–
10	0.431	–1.86	29.19	0	0.779	9.94	67.5	2.22
20	0.441	–4.06	29.20	–0.039	0.698	19.3	66.2	4.23
30	0.450	–6.3	29.23	–0.14	0.622	28.2	64.9	6.31

^a Relaxation values were calculated assuming $S^2 = 0.85$ and $\tau_R = 20$ ns

^b “Diff” indicates a fractional difference, $(X^{\text{SMF}} - X^{\text{MF}})/X^{\text{MF}}$. Here, X can be R_1 , R_2 , NOE, or R_2/R_1

Values at $\tau_i = 0$ corresponds to the case of $X^{\text{SMF}} = X^{\text{MF}}$

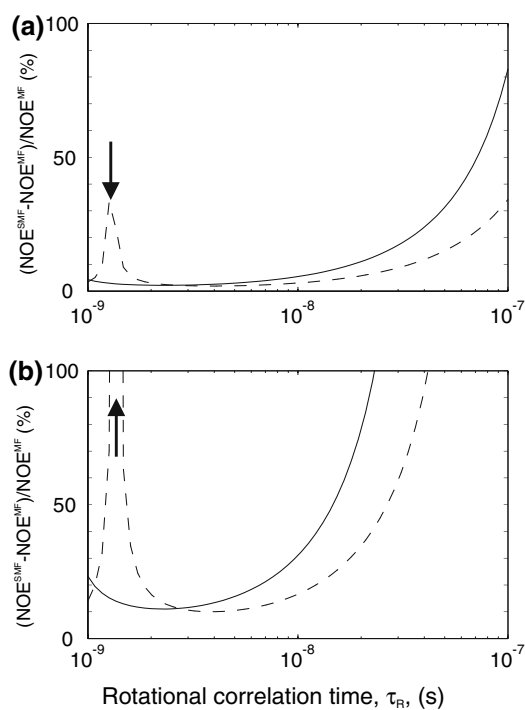


Fig. 4 Percentage difference of NOE values, $\{(\text{NOE}^{\text{SMF}} - \text{NOE}^{\text{MF}}) / \text{NOE}^{\text{MF}}\}$, assuming at (a) $\tau_i = 10$ ps and (b) 50 ps. Arrows indicates the point that the sign of the NOE is changed. Solid lines are those calculated at 18.8 T, and dashed lines are those calculated at 11.74 T. NOE^{SMF} and NOE^{MF} indicates NOE values calculated using $J_{\text{SMF}}(\omega)$ and $J_{\text{MF}}(\omega)$, respectively. S^2 and R_{ex} were assumed to be 0.85 and 0, respectively

that the $R_2^{\text{SMF}}/R_1^{\text{SMF}}$ values are slightly larger than $R_2^{\text{MF}}/R_1^{\text{MF}}$ values, which is reasonable since R_1^{SMF} values are slightly smaller than R_1^{MF} (Fig. 2a) and since the R_2^{SMF} values are similar to the R_2^{MF} (Eqs. 2 and 8).

The differences in R_2/R_1 values, $\{(R_2^{\text{SMF}}/R_1^{\text{SMF}}) - (R_2^{\text{MF}}/R_1^{\text{MF}})\} / (R_2^{\text{MF}}/R_1^{\text{MF}})$, are less than 2% at $\tau_i = 10$ ps and

$\tau_R = 10$ ns, at either 11.74 or 18.8 T (Fig. 5a). However, the discrepancy becomes more significant when $\tau_i = 50$ ps (Fig. 5b). When $\tau_R = 20$ ns at 18.8 T, the R_2/R_1 value calculated using $J_{\text{SMF}}(\omega)$ differs 9.4% from that calculated using $J_{\text{MF}}(\omega)$. Thus, when τ_R value is determined directly by calculating $R_2^{\text{SMF}}/R_1^{\text{SMF}}$, τ_R will be 4.6% underestimated. If S^2 is determined primarily by the contribution from the R_2 as suggested by Eqs. 2 and 8, then, it will be

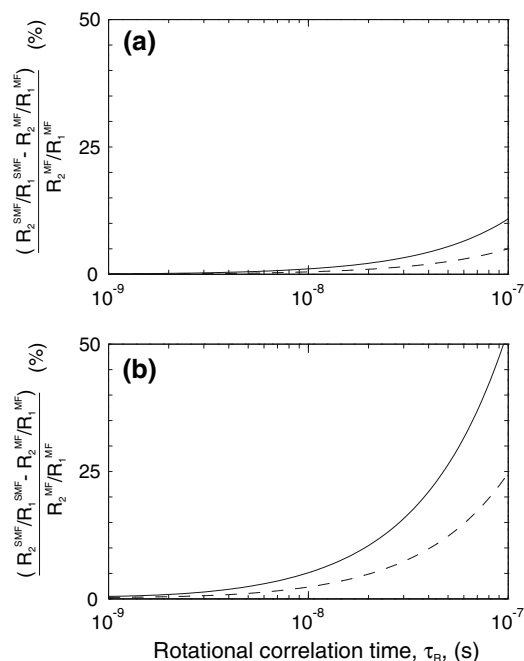


Fig. 5 Percentage difference of R_2/R_1 values, $(R_2^{\text{SMF}}/R_1^{\text{SMF}} - R_2^{\text{MF}}/R_1^{\text{MF}}) / (R_2^{\text{MF}}/R_1^{\text{MF}})$, assuming at (a) $\tau_i = 10$ ps and (b) 50 ps. Solid lines are those calculated at 18.8 T, and dashed lines are those calculated at 11.74 T. S^2 and R_{ex} were assumed to be 0.85 and 0, respectively

overestimated due to the underestimation of τ_R . Thus, in the case of high field model-free analysis of larger proteins, it is suggested that τ_R values be estimated by fitting with $J_{MF}(\omega)$ for the sites closest to the trimmed mean R_2/R_1 value (Clore et al. 1990; Schneider et al. 1992) rather than by assuming $J_{SMF}(\omega)$.

Use of $J_{SMF}(\omega)$ at high magnetic field experiments for large proteins

Here, we show that R_1 and NOE values calculated using $J_{SMF}(\omega)$ become significantly different from those calculated using $J_{MF}(\omega)$ when the magnetic field strength or the rotational correlation time increases. When $J_{SMF}(\omega)$ is applied to optimize the model-free parameters at each amide site, the $S^2\tau_R/(1 + \omega_N^2\tau_R^2)$ term has to compensate for the neglect of the contribution from the $(1-S^2)\tau_e/(1 + \omega_H^2\tau_e^2)$ term in the $J_{MF}(\omega)$ spectral density, which results in an overestimation of S^2 . Additionally, significant differences in R_1 will also influence the estimation of τ_R when it is directly calculated from the average R_2/R_1 ratio.

In practice, it is difficult to assess the accuracy of the optimized parameters when simplified model-free analysis is used to analyze very complicated protein dynamics (Andrec et al. 1999; Barchi et al. 1994; Chandrasekhar et al. 1992; Chen et al. 2004; d’Auvergne and Gooley 2003; Korchuganov et al. 2004; Korzhnev et al. 1997; Lee and Wand 1999; Meirovitch et al. 2003; Pawley et al. 2001; Schramm et al. 1991; Spyrapoulos 2006). In particular, contributions from R_{ex} , slow internal motion, and molecular anisotropy will each make evaluation of the R_2/R_1 ratio difficult. In addition, there are many factors that can influence the experimental values of heteronuclear NOE (Gong and Ishima 2007; Grzesiek and Bax 1993; Li and Montelione 1994; Renner et al. 2002; Skelton et al. 1993). Particularly, insufficient magnetization recovery will increase the NOE values, which in turn may cancel the reduction of NOE value caused by internal motion. Finally, even when $J_{MF}(\omega)$ model is applied for rigid sites, it is uncertain the extent to which $J_{MF}(\omega)$ differs from the actual spectral density at that site.

In spite of these difficulties, some of the published data, ubiquitin and TEM-1 in Table 2, clearly show a tendency that τ_R values estimated based on R_2/R_1 decrease as the magnetic field strength increases, which is consistent with our prediction. This reduction of the rotational correlation time estimated based on the $J_{SMF}(\omega)$ spectral density may reflect the difference between a real spectral density of a protein and $J_{MF}(\omega)$ spectral density. Although such differences are relatively small, 2–3%, for the data considered here, they might have a significant impact if the differences are directly reflected in the S^2 values. In

contrast, the rotational correlation times of km23 (27 kDa homodimeric protein) estimated based on the $J_{MF}(\omega)$ spectral density increased as the magnetic field strength increased (Table 2), which may be due to residual chemical exchange contribution to R_2 .

To avoid bias caused by R_1/R_2 ratio (or $J_{SMF}(\omega)$), the following strategies that are essentially free from the internal motion of each site may be applied when $\omega\tau_e \ll 1$.

$$J_{MF}(\omega) \cong S^2 \frac{\tau_R}{(1 + \omega^2\tau_R^2)} + (1 - S^2)\tau_e = J_{SMF}(\omega) + (1 - S^2)\tau_e \tag{10}$$

Using the notation shown in Eq. 10, relaxation rates are described by the following equations.

$$R_1^{MF} = R_1^{SMF} + (d^2 + c^2)(1 - S^2)\tau_e \tag{11}$$

$$R_2^{MF} = R_2^{SMF} + (d^2 + 7c^2/6)(1 - S^2)\tau_e \tag{12}$$

$$\sigma_{cross}^{MF} = \sigma_{cross}^{SMF} + (d^2/2)(1 - S^2)\tau_e \tag{13}$$

Based on these equations, an R_1/R_2 ratio that does not contain $(1-S^2)\tau_e$ term is derived.

$$\frac{R_2 - 2\sigma(d^2 + 7c_2/6)/d^2}{R_1 - 2\sigma(d^2 + c_2)/d^2} = \frac{R_2^{SMF} - 2\sigma^{SMF}(d^2 + 7c_2/6)/d^2}{R_1^{SMF} - 2\sigma^{SMF}(d^2 + c_2)/d^2} \tag{14}$$

This concept is recast in a simpler form using reduced spectral density function (Ishima and Nagayama 1995; Lefevre et al. 1996; Peng and Wagner 1995). Equation 10 clearly indicates that subtraction of the spectral density functions cancels out the $(1-S^2)\tau_e$ terms. Thus, τ_R is described by,

$$\tau_R = \left(\frac{(J(0) - J(\omega_N))}{(J(\omega_N) - J(\omega_H))} \cdot \frac{(0.87^* \omega_H - \omega_N)^2}{\omega_N^2} - 1 \right)^{1/2} / \omega_H \tag{15}$$

The coefficient, 0.87, is a correction value in the reduced spectral density function (Pfeiffer et al. 2001). This equation is very similar to the equation previously derived (Fushman et al. 1994), but more generalized such that motion at ω_H does not affect τ_R (Fushman and Cowburn 2001). This equation is also similar to that described by Kroenke et al. (1998), but differs in that the $(1-S^2)\tau_e$ term is selectively removed rather than eliminating the entire $J(\omega_H)$ term. τ_R values were calculated using Eqs. 14 and 15 for km23 and TEM-1 (Table 2) and

Table 2 Rotational correlation times estimated using different methods^{d,e}

km23 (Ilangoan et al. 2005) ^a	14.09 T	16.45 T	
Number of residues among total	39/83	37/83	
Average R_1	1.23 (0.066)	1.03 (0.045)	
Average R_2	13.64 (1.1)	15.75 (1.1)	
Average NOE	0.808 (0.038)	0.803 (0.049)	
τ_R estimated from R_2/R_1 ratio (ns)	10.25 (–)	10.45 (–)	
τ_R estimated from fit using $J_{SMF}(\omega)$ (ns)	10.25 (0.02)	10.45 (0.02)	
τ_R estimated from fit using $J_{MF}(\omega)$ (ns)	10.52 (0.05)	10.76 (0.03)	
τ_R estimated using Eq. 14	10.28 (0.05)	10.53 (0.03)	
τ_R estimated using Eq. 15	10.20	10.51	
Ubiquitin (Chang and Tjandra 2005) ^b	14.09 T	18.8 T	
Number of residues among total	53/64	38/63	
Average R_1	1.91 (0.066)	1.47 (0.038)	
Average R_2	7.60 (0.416)	8.70 (0.523)	
τ_R estimated from R_2/R_1 ratio (ns)	5.45 (0.19)	5.31 (0.20)	
τ_R estimated from fit using $J_{SMF}(\omega)$ (ns)	5.45 (0.04)	5.30 (0.05)	
TEM-1 (Savard and Gagne 2006) ^c	11.74 T	14.09 T	18.8 T
τ_R estimated from R_2/R_1 ratio (ns)	12.74	12.64	12.33
τ_R estimated from fit using $J_{SMF}(\omega)$ (ns)	12.7	12.5	–
τ_R estimated from fit using $J_{MF}(\omega)$ (ns)	12.82	12.76	–
τ_R estimated using Eq. 14	12.85	12.75	–
τ_R estimated using Eq. 15	12.93	12.80	–

^a Km23 data published previously were used for the analysis (Ilangoan et al. 2005)

^b Ubiquitin data are basically the same as published previously but obtained using ¹⁵N protein (Chang and Tjandra 2005)

^c TEM-1 data was obtained from the literature (Savard and Gagne 2006) and analyzed only using average R_1 , R_2 , and NOE values

^d Numbers in parentheses in R_1 , R_2 , NOE, and τ_R values indicate uncertainty

^e Residues for analysis were selected to satisfy the following four conditions (i) the NOE > 0.7, (ii) R_1 is within 1.5 standard deviation, (iii) R_2/R_1 is within 1 standard deviation, and (iv) $(R_2 - \langle R_2 \rangle) / (R_2 - (R_1 - \langle R_1 \rangle)) / \langle R_1 \rangle$ is smaller than 1.5 standard deviation. Since NOE values were not obtained for the ubiquitin data, residues for analysis for ubiquitin were selected to satisfy the above criteria, without (i) but using 0.5 standard deviation for (iii)

with the former were found to be close to those calculated using $J_{MF}(\omega)$, which is expected since these methods assume the same spectral density function. τ_R values calculated using the latter differed slightly from those calculated using $J_{MF}(\omega)$ presumably due to inaccuracies in some of the assumptions used to derive the reduced spectral density function.

Acknowledgements We thank Dennis Torchia and Nico Tjandra for critical reading of the manuscript. Financial support for this work was provided by University of Pittsburgh to R.I., and the NIH and the Robert A. Welch Foundation to A.H.

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